

1) A particle is moving with its position defined by $s(t) = 2t^3 + 3t^2 - 20t + 6$ where t is in seconds and s is in feet.

- What are the particle's velocity and acceleration functions?
- What is the total distance traveled by the particle in the first three seconds?
- What is the displacement of the particle after the first eight seconds?

$$a) s(t) = 2t^3 + 3t^2 - 20t + 6$$

$$v(t) = 6t^2 + 6t - 20$$

$$a(t) = 12t + 6$$

$$b) s(0) = 6 \text{ ft.}$$

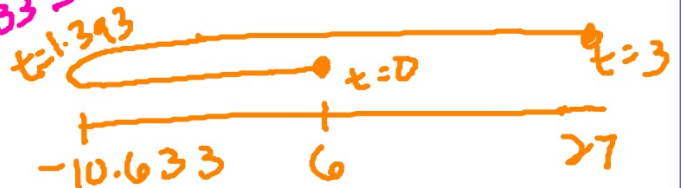
$$s(1.393) = -10.633 \text{ ft.}$$

$$s(3) = 27 \text{ ft.}$$

$$\left. \begin{array}{l} 16.633 \\ 37.633 \end{array} \right\} \boxed{54.266 \text{ ft}}$$

$$6t^2 + 6t - 20 = 0$$

$$t = 1.393$$



c) Displacement $0 \rightarrow 8 \text{ sec.}$

$$s(0) = 6 \text{ ft.}$$

$$s(8) = 1062 \text{ ft.}$$

$\boxed{1,056 \text{ ft to the right}}$

2) A silver dollar is dropped from a building that is 1,362 feet in height. Time is in seconds.

a) What are the silver dollar's height, velocity and acceleration functions?

$$a) s(t) = -16t^2 + 1362$$

$$v(t) = -32t$$

$$a(t) = -32$$

b) When does the silver dollar hit the ground and what is its impact velocity?

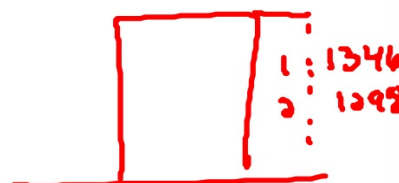
c) How far does the silver dollar travel between $t=1$ second and $t=2$ seconds?

$$b) -16t^2 + 1362 = 0$$

$$t = 9.226 \text{ sec}$$

$$v(9.226) = -295.232 \text{ ft/sec}$$

$$c) \begin{matrix} s(1) = 1346 \\ s(2) = 1298 \end{matrix} \quad \boxed{48 \text{ ft}}$$



3) The displacement in feet of a body moving along a line at any time t in seconds is given by $s(t) = t^3 - 7t^2 + 8t + 4$.

- What are the velocity and acceleration functions?
- Find the total distance traveled from $t=0$ second to $t=5$ seconds.
- What is the velocity of the body when the position is 8 feet?
- Sketch a motion schematic. Be sure to label the time, position, and velocity at each change and at the beginning.

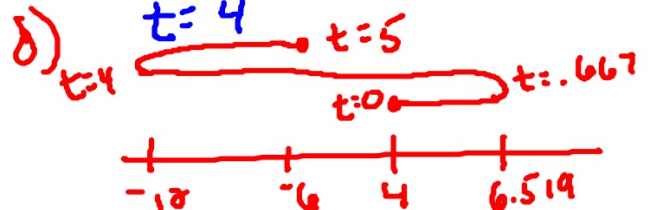
$$a) v(t) = 3t^2 - 14t + 8$$

$$a(t) = 6t - 14$$

$$3t^2 - 14t + 8 = 0$$

$$t = .667$$

$$t = 4$$



$$b) s(0) = 4$$

$$s(.667) = 6.519$$

$$s(4) = -12$$

$$s(5) = -6$$

$$2.519$$

$$18.519$$

$$6$$

$$27.038 \text{ ft.}$$

$$c) t^3 - 7t^2 + 8t + 4 = 8$$

$$t = 5.725 \text{ sec.}$$

$$v(5.725) = 26.177 \text{ ft/sec}$$

4) A marble is thrown straight down from the top of a 220-foot building. Its initial velocity was 22 feet per second.

- a) What are the marble's height, velocity, and acceleration functions?
- b) When does the marble hit the ground and what is its impact velocity?
- c) What are the velocity and position at three seconds?
- d) What is its velocity after falling 108 feet?

$$b) -16t^2 - 22t + 220 = 0$$

$$t = 3.084 \text{ sec.}$$

$$v(3.084) = -170.688 \text{ ft/sec}$$

$$c) s(3) = 10 \text{ ft}$$

$$v(3) = -118 \text{ ft/sec.}$$

$$a) s(t) = -16t^2 - 22t + 220$$

$$v(t) = -32t - 22$$

$$a(t) = -32$$

$$d) -16t^2 - 22t + 220 = 112$$

$$t = 2 \text{ sec}$$

$$v(2) = -86 \text{ ft/sec}$$

An object has its position defined by $s(t) = t^3 - 5t^2 + 5t + 2$ feet. Time is in seconds.

- a) What are the velocity and acceleration functions?
- b) What is the total distance traveled by the object during the first eight seconds?
- c) What is the displacement of the object after the first eight seconds?
- d) What is the position when the velocity is 3.1 feet per second?
- e) What is the velocity when the acceleration is -2.7 feet per second²?

A bag of sugar is launched vertically upward from a height of 5 feet with an initial velocity of 102 feet per second.

- a) What are the bag's height, velocity, and acceleration functions?
- b) What is the position of the bag when the velocity is 22 feet per second?
- c) When will the bag hit the ground? What is its impact velocity?
- d) When will the bag reach its maximum height? What is its maximum height?